## Mark Scheme (Results) January 2010

## GCE

## Statistics S2 (6684)

Edexcel is one of the leading examining and awarding bodies in the UK and throughout the world. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers.
Through a network of UK and overseas offices, Edexcel's centres receive the support they need to help them deliver their education and training programmes to learners.
For further information, please call our GCE line on 0844576 0025, our GCSE team on 0844576 0027, or visit our website at www.edexcel.com.

If you have any subject specific questions about the content of this Mark Scheme that require the help of a subject specialist, you may find our Ask The Expert email service helpful.

Ask The Expert can be accessed online at the following link:
http:/ / www.edexcel.com/ Aboutus/ contact-us/

January 2010
Publications Code UA023029
All the material in this publication is copyright
© Edexcel Ltd 2010

January 2010
6684 Statistics S2
Mark Scheme

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q1 (a) <br> (b) <br> (c) <br> (d) | $X \sim B(20,0.05)$ <br> $\mathrm{P}(\mathrm{X}=0)=0.95^{20}=0.3584859 \ldots$ or 0.3585 using tables . $\begin{aligned} \mathrm{P}(X>4) & =1-\mathrm{P}(X \leq 4) \\ & =1-0.9974 \\ & =0.0026 \end{aligned}$ $\begin{aligned} & \text { Mean }=20 \times 0.05=1 \\ & \text { Variance }=20 \times 0.05 \times 0.95=0.95 \end{aligned}$ | B1 B1  <br> M1 A1 (2) <br> M1  <br> (2)  <br> A1  <br>   <br> B1  <br> B1  <br> (2)  <br> Total [8]  |
| (b) <br> (c) <br> (d) | Notes <br> $\mathbf{1}^{\text {st }} \mathbf{B 1}$ for binomial <br> $\mathbf{2}^{\text {nd }} \mathbf{B 1}$ for 20 and 0.05 o.e <br> These must be in part (a) <br> M1 for finding $(p)^{20} \quad 0<p<1 \quad$ this working needs to be seen if answer incorrect to gain the M1 <br> A1 awrt 0.358 or 0.359 . <br> M1 for writing 1-P $(X \leq 4)$ <br> or $1-[\mathrm{P}(X=0)+\mathrm{P}(X=1)+\mathrm{P}(X=2)+\mathrm{P}(X=3)+\mathrm{P}(X=4)]$ <br> or $1-0.9974$ <br> or $1-0.9568$ <br> A1 awrt 0.0026 or $2.6 \times 10^{-3}$, do not accept a fraction e.g. 26/10000 <br> $\mathbf{1}^{\text {st }} \mathbf{B 1}$ for 1 <br> $\mathbf{2}^{\text {nd }} \mathbf{B 1}$ for 0.95 <br> NB In parts $\mathrm{b}, \mathrm{c}$ and d correct answers with no working gain full marks |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q2 ${ }^{(a)}$ | $\mathrm{P}(X<0) \quad=\mathrm{F}(0)$ | M1 |
|  | $=\frac{2}{6}=\frac{1}{3}$ | A1 (2) |
|  | $\mathrm{f}(x)=\frac{\mathrm{dF}(x)}{\mathrm{d} x}$ | M1 |
|  | $\mathrm{f}(x)=\left\{\begin{array}{cc} \frac{1}{6} & -2 \leq x \leq 4 \\ 0 & \text { otherwise } \end{array}\right.$ | $\begin{aligned} & \mathrm{A} 1 \\ & \mathrm{~B} 1 \end{aligned}$ |
|  |  | (3) |
|  | Continuous Uniform (Rectangular) distribution | B1 (1) |
|  | Mean $=1$ | B1 |
|  | Variance is $\frac{(4--2)^{2}}{12}=3$ | M1 A1 |
|  | $\mathrm{P}(X=1)=0$ | B1 |
|  |  | (1) |
|  |  | Total [10] |
| Q2 ${ }^{(a)}$ | Notes |  |
|  | M1 for attempting to find $\mathrm{F}(0)$ by a correct method eg subst 0 into $\mathrm{F}(x)$ or $\int_{-2}^{0} \frac{1}{6} d x$ <br> Do NOT award M1 for $\int_{-2}^{0} \frac{x+2}{6} d x$ or $\frac{1}{2} \times \frac{1}{3} \times 2$ both of which give the correct answer by using $\mathrm{F}(x)$ as the pdf <br> A1 $1 / 3$ o.e or awrt 0.333 <br> Correct answer only with no incorrect working gets M1 A1 |  |
|  | M1 for attempting to differentiate $\mathrm{F}(x)$. (for attempt it must have no $x \mathrm{~s}$ in) A1 for the first line. Condone < signs B1 for the second line. - They must have $0 x<-2$ and $x>4$ only. |  |
|  | B1 must have "continuous" and "uniform" or "Rectangular" |  |
|  | $\mathbf{B} 1 \text { for mean }=1$ |  |
|  | M1 for attempt to use $\frac{[ \pm(b-a)]^{2}}{12}$, they must subst in values and not just quote the formula, or using $\int_{-2}^{4} x^{2}($ their $f(x))-(\text { their mean })^{2}$, including limits. Must get $x^{3}$ when they integrate. <br> A1 cao. |  |
|  | B1 cao |  |




## Notes

Q4 (a) $\mathbf{1}^{\text {st }} \mathbf{M 1}$ attempting to integrate at least one part (at least one $x^{n} \rightarrow x^{n+1}$ ) (ignore limits)
$1^{\text {st }}$ A1 Correct integration. Limits not needed.
$\mathbf{2}^{\text {nd }} \mathbf{M 1}$ dependent on the previous $M$ being awarded. Adding the two answers together, putting equal to 1 and have the correct limits.
$2^{\text {nd }} \mathrm{A} 1$ cso
(b)
$\mathbf{1}^{\text {st }}$ M1 Att to integrate $\frac{1}{9}\left(t^{2}-2 t+2\right)$ (at least one $\left.x^{n} \rightarrow x^{n+1}\right)$. Ignore limits for method mark
$\mathbf{1}^{\text {st }}$ A1 $\frac{1}{9}\left(\frac{x^{3}}{3}-x^{2}+2 x\right)$ allow use of $t$. Must have used/implied use of limit of 0 . This must be on its own without anything else added
$\mathbf{2}^{\text {nd }} \mathbf{M 1}$ attempting to find $\int_{3}^{x} 3 k+\ldots$ (must get $3 k t$ or $3 k x$ )
and they must use the correct limits and add $\int_{0}^{3} \frac{1}{9}\left(t^{2}-2 t+2\right)$ or $\frac{2}{3}$
or use +C and use $\mathrm{F}(4)=1$
$\mathbf{2}^{\text {nd }} \mathbf{A 1} \frac{x}{3}-\frac{1}{3}$ must be correct
$\mathbf{1}^{\text {st }} \mathbf{B 1}$ middle pair followed through from their answers. condone them using <or $\leq$ incorrectly they do not need to match up
$\mathbf{2}^{\text {nd }} \mathbf{B 1}$ end pairs. condone them using < or $\leq$. They do not need to match up
NB if they show no working and just write down the distribution. If it is correct they get full marks. If it is incorrect then they cannot get marks for any incorrect part. So if $0<x \leq 3$ is correct they can get M1 A1 otherwise M0 A0. If $3<x \leq 4$ is correct they can get M1 A1 otherwise M0 A0. you cannot award B1ft if they show no working unless the middle parts are correct.
(c)
$\mathbf{1}^{\text {st }}$ M1 attempting to use integral of $x \mathrm{f}(x)$ on one part
$\mathbf{1}^{\text {st }} \mathbf{A 1}$ Correct Integration for both parts added together. Ignore limits.
$\mathbf{2}^{\text {nd }} \mathbf{A 1}$ cao or awrt 2.42
(d) $\quad \mathbf{1}^{\text {st }} \mathbf{M 1}$ for using $\mathrm{F}(X)=0.5$. This may be implied by subst into $\mathrm{F}(X)$ and comparing answers with 0.5 .
$\mathbf{2}^{\text {nd }} \mathbf{M 1}$ for substituting both 2.6 and 2.7 into "their $\mathrm{F}(X)$ " -0.5 or "their $\mathrm{F}(X)$ "
$\mathbf{1}^{\text {st }} \mathbf{A 1}$ awrt 0.48 and 0.52 if using "their $\mathrm{F}(X)$ "
and awrt -0.02 and 0.02 or if using "their $\mathrm{F}(\mathrm{X})$ " 0.5
Other values possible. You may need to check their values for their correct equation
NB these last two marks are B1 B1 on ePEN but mark as M1 A1
$\mathbf{2}^{\text {nd }} \mathbf{A 1}$ for conclusion but only award if it follows from their numbers. Dependent on previous A mark being awarded
SC using calculators
M1 for sign of a suitable equation
M1 A1 for awrt 2.66 provided equation is correct
A1 correct comment

| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| Q5 (a) <br> (b) | $\begin{array}{ll} X \sim \operatorname{Po}(10) & \\ \mathrm{P}(X<9) & =\mathrm{P}(X \leq 8) \\ & =0.3328 \end{array}$ $Y \sim \operatorname{Po}(40)$ <br> $Y$ is approximately $\mathrm{N}(40,40)$ $\begin{aligned} \mathrm{P}(Y>50) \quad & =1-\mathrm{P}(Y \leq 50) \\ & =1-\mathrm{P}\left(Z<\frac{50.5-40}{\sqrt{40}}\right) \\ & =1-\mathrm{P}(Z<1.660 . .) \\ & =1-0.9515 \\ & =0.0485 \end{aligned}$ <br> N.B. Calculator gives 0.048437 . <br> Poisson gives 0.0526 (but scores nothing) | B1 <br> M1 <br> A1 <br> (3) <br> M1 A1 <br> M1 <br> M1 <br> A1 <br> A1 <br> (6) <br> Total [9] |
| Q5 (a) <br> (b) | Notes <br> B1 for using Po(10) <br> M1 for attempting to find $\mathrm{P}(X \leq 8)$ : useful values $\mathrm{P}(X \leq 9)$ is 0.4579 (M0), using $\mathrm{Po}(6)$ gives 0.8472 , (M1). <br> A1 awrt 0.333 but do not accept $\frac{1}{3}$ <br> $\mathbf{1}^{\text {st }} \mathbf{M 1}$ for identifying the normal approximation <br> $\mathbf{1}^{\text {st }} \mathbf{A 1}$ for [mean $\left.=40\right]$ and $[\mathrm{sd}=\sqrt{40}$ or var $=40$ ] <br> NB These two marks are B1 M1 on ePEN <br> These first two marks may be given if the following are seen in the standardisation formula : 40 and $\sqrt{40}$ or awrt 6.32 <br> $\mathbf{2}^{\text {nd }} \mathbf{M 1}$ for attempting a continuity correction ( 50 or $30 \pm 0.5$ is acceptable) <br> $\mathbf{3}^{\text {rd }}$ M1 for standardising using their mean and their standard deviation and using either $49.5,50$ or 50.5 . $(29.5,30,30.5)$ accept $\pm$ <br> $2^{\text {nd }} \mathbf{A 1}$ correct z value awrt $\pm 1.66$ or this may be awarded if see $\pm \frac{50.5-40}{\sqrt{40}}$ or $\pm \frac{29.5-40}{\sqrt{40}}$ <br> $\boldsymbol{3}^{\text {rd }} \mathbf{A 1}$ awrt 3 sig fig in range $0.0484-0.0485$ |  |


| Question Number | Scheme | Marks |
| :---: | :---: | :---: |
| (b) <br> (c) <br> (d) | The set of values of the test statistic for which the null hypothesis is rejected in a hypothesis test. $\begin{align*} & X \sim \mathrm{~B}(30,0.3) \\ & \mathrm{P}(X \leq 3)=0.0093 \\ & \mathrm{P}(X \leq 2)=0.0021 \\ & \mathrm{P}(X \geq 16)=1-0.9936=0.0064 \\ & \mathrm{P}(X \geq 17)=1-0.9979=0.0021 \tag{5} \end{align*}$ <br> Critical region is $(0 \leq) x \leq 2$ or $16 \leq x(\leq 30)$ <br> Actual significance level $0.0021+0.0064=0.0085$ or $0.85 \%$ <br> 15 (it) is not in the critical region <br> not significant <br> No significant evidence of a change in $p=0.3$ <br> accept $\mathrm{H}_{0}$, (reject $\mathrm{H}_{1}$ ) $\mathrm{P}(x \geq 15)=0.0169$ | B1 <br> B1 <br> (2) <br> M1 <br> A1 <br> A1 <br> A1A1 <br> B1 <br> (1) <br> Bft 2, 1, 0 <br> (2) |
| (b) <br> (c) <br> (d) | Notes <br> $1^{\text {st }} \mathrm{B} 1$ for "values/ numbers" <br> $\mathbf{2}^{\text {nd }} \mathbf{B 1}$ for "reject the null hypothesis" o.e or the test is significant <br> M1 for using $\mathrm{B}(30,0.3)$ <br> $\mathbf{1}^{\text {st }} \mathbf{A 1} \mathrm{P}(x \leq 2)=0.0021$ <br> $2^{\text {nd }} \mathbf{A 1} 0.0064$ <br> $\mathbf{3}^{\text {rd }} \mathbf{A 1}$ for $(X) \leq 2$ or $(X)<3 \quad$ They get $\mathbf{A 0}$ if they write $\mathbf{P}(X \leq 2 / X<3)$ <br> $\mathbf{4}^{\text {th }} \mathbf{A 1}(X) \geq 16$ or $(X)>15$ They get A0 if they write $\mathbf{P}(X \geq 16 X>15$ <br> NB these are B1 B1 but mark as A1 A1 <br> $16 \leq X \leq 2$ etc is accepted <br> To describe the critical regions they can use any letter or no letter at all. It does not have to be $X$. <br> B1 correct answer only <br> Follow through 15 and their critical region <br> B1 for any one of the 5 correct statements up to a maximum of B2 <br> -B1 for any incorrect statements |  |



Further copies of this publication are available from
Edexcel Publications, Adamsway, Mansfield, Notts, NG18 4FN
Telephone 01623467467
Fax 01623450481

Email publications@inneydirect.com
Order Code UA023029 January 2010

For more information on Edexcel qualifications, please visit www.edexcel.com/quals

Edexcel Limited. Registered in England and Wales no. 4496750
Registered Office: One90 High Holborn, London, WC1V 7BH

